

# Lecture #8 : Tolerance analysis

1. Importance of tolerance analysis
2. Fundamentals of tolerance
  - o Tolerance and normal distribution
  - o  $6\sigma$ , Cp, and Cpk
  - o Yield rate and DPU
  - o Poisson distribution
3. Approach to  $6\sigma$  design and production
4. An example : Tunable filter design
  - o Description of the tunable filter design
  - o Monte-Carlo analysis
5. Appendix: Table of normal probability function

## 1. Importance of tolerance analysis

- o Tolerance analysis is not important for a prototype design in the Laboratory but, it is very important for a product in the massive production line.
- o The existence of a product in massive production line depends mainly on the yield rate of the product
- o Yield rate of a product is mostly determined by the tolerance of all the parts.
- o The tool of the tolerance analysis in the simulation stage of design is “Monte Carlo”.
- o In some circuit designs, the performance are mainly limited by the tolerance. The designer must do the tolerance analysis first.

The following example, a tunable filter design, illustrates the first priority of the tolerance analysis.



Richard Li, 2006

## 2. Fundamentals of tolerance

### o Plot of relative number of resistors versus value of resistor

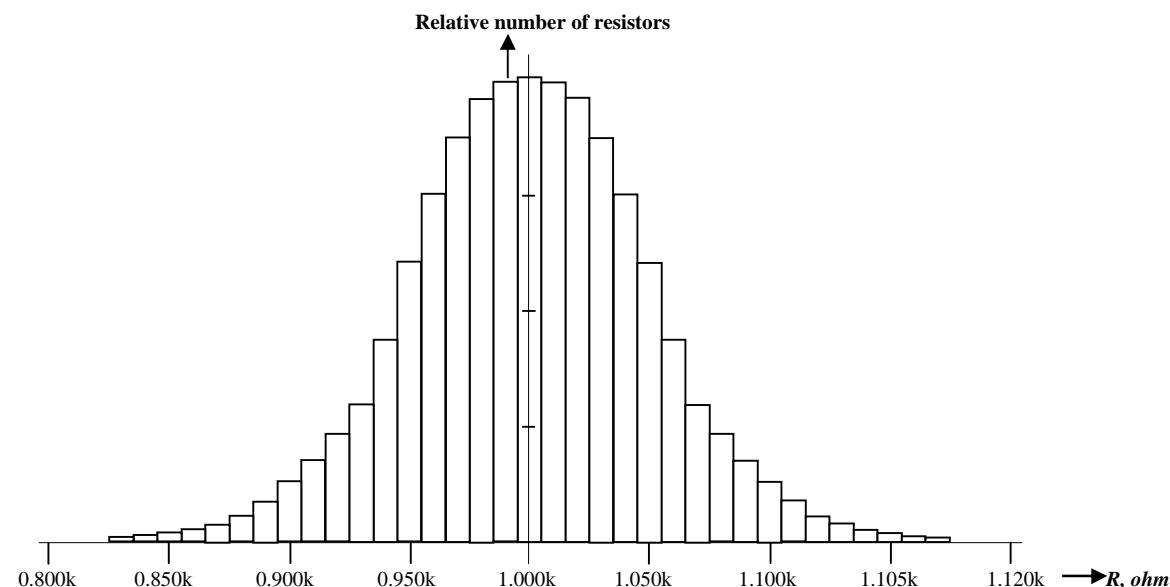


Figure 8.1 Histogram of relative number of resistors versus the value of resistor

## o Gaussian probability function

\* Sample value :

$$R_i ,$$

\* Average value :

$$m = 1000 \text{ ohms} ,$$

\* Relative tolerance :

$$Tol_{\text{Relative}} = \frac{\sqrt{\sum_i \Delta R_i^2}}{m} = \frac{s}{m} = 5\% ,$$

\* Variance or standard deviation

$$s = \sqrt{\sum_i \Delta R_i^2} \text{ ohms} .$$

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\* Gaussian distribution :

$$f(z) = \int_0^z r(x) dx = \int_0^z \frac{e^{-\frac{x^2}{2s^2}}}{\sqrt{2\pi}} dx$$

where

$$z = \frac{R-m}{s}$$
$$r(x) = \frac{e^{-\frac{x^2}{2s^2}}}{\sqrt{2\pi}}$$

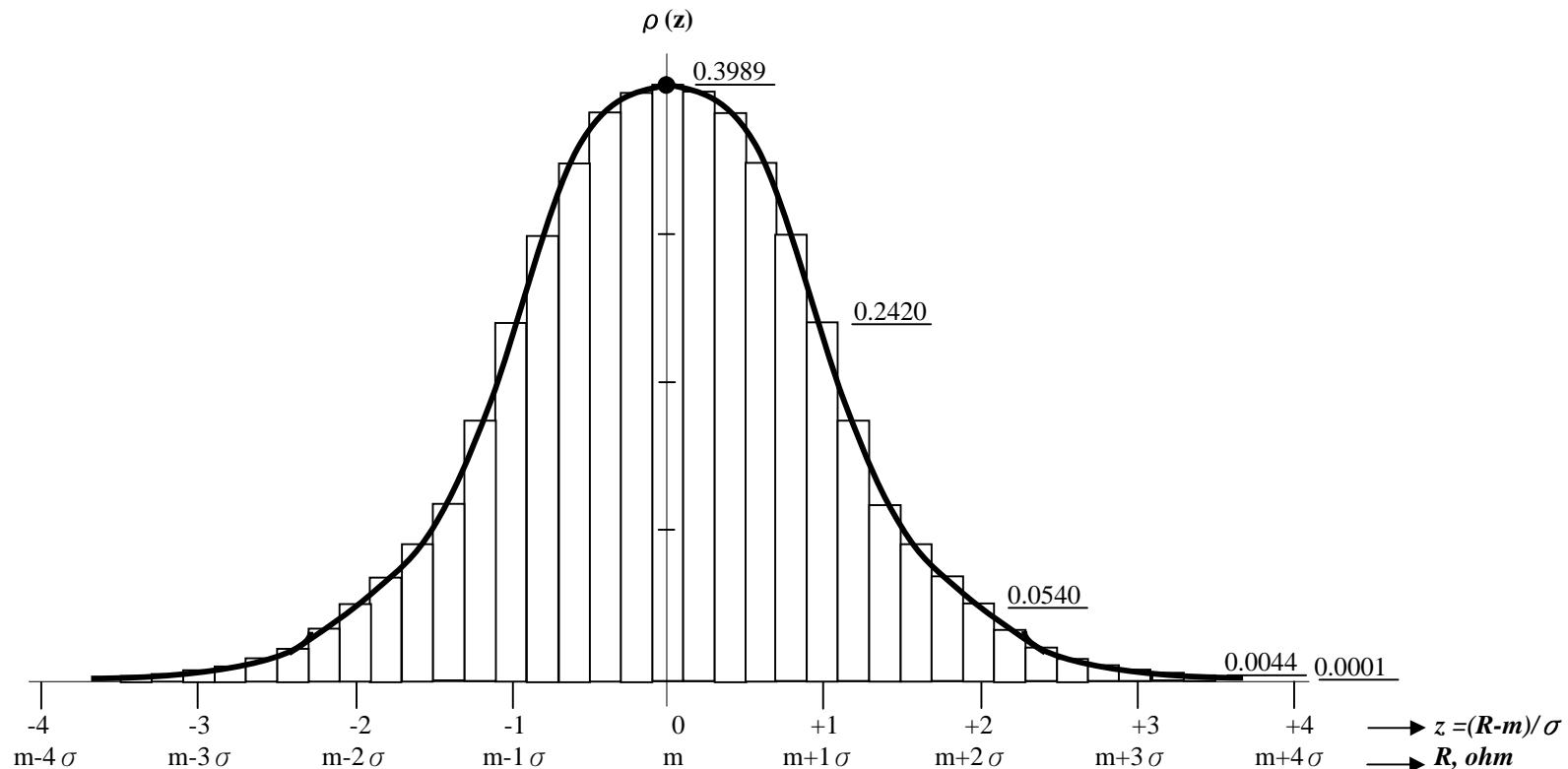


Figure 8.2 Distribution of the random variable,  $R$ , is a Normal probability function or a Gaussian distribution

## o Tolerance and normal distribution

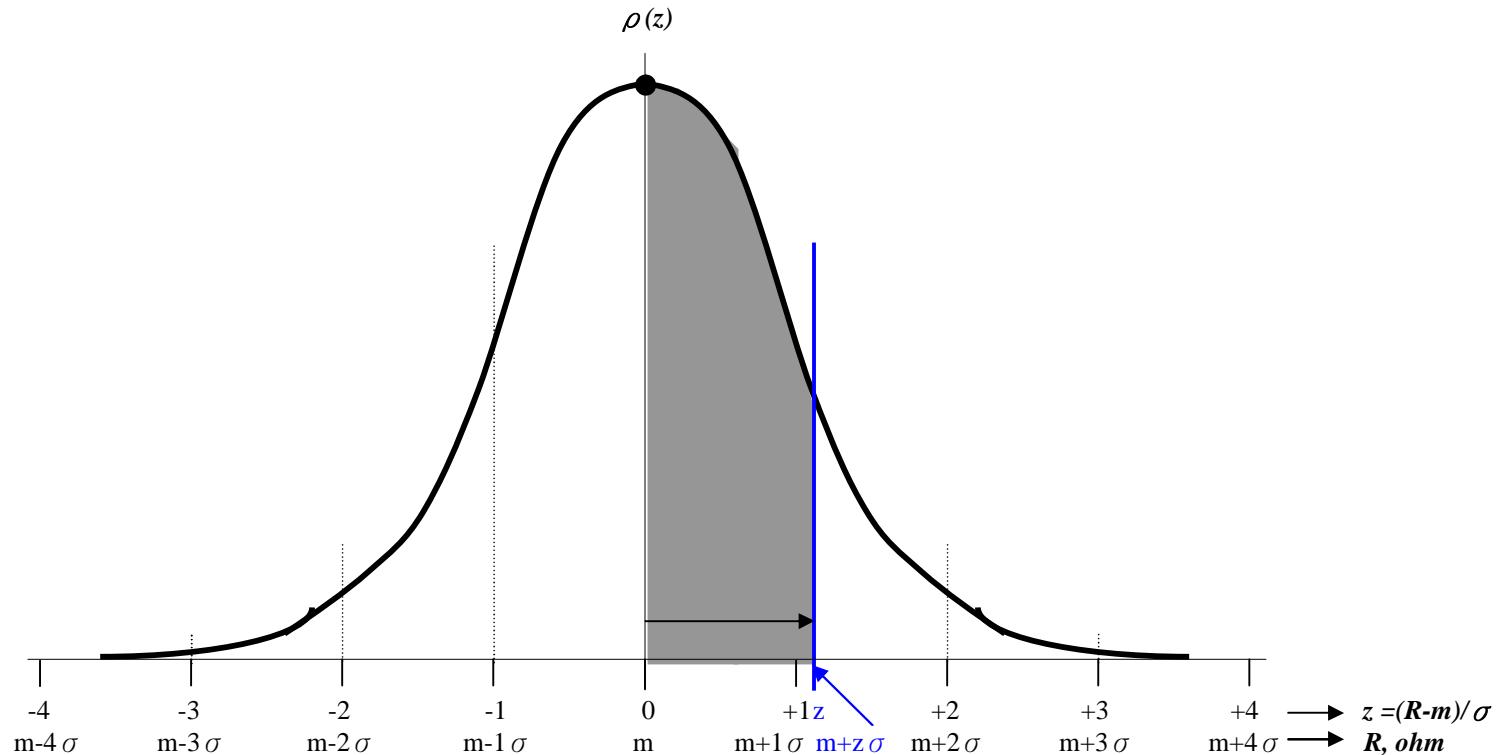


Figure 8.3 Integral of  $\rho(z)$  from 0 to  $z$  or from  $m$  to  $m+z\sigma$ .

## o Six sigma and 100% yield rate

Gaussian distribution :

$$f(z) = \int_0^z \frac{e^{-\frac{(x-m)^2}{2s^2}}}{\sqrt{2\pi s^2}} dx$$

where  $m$  = average of the variable  $x$  ;  
 $\sigma$  = square root of the variable  $x$ .

Normal probability function is a Gaussian distribution function  
when :  $m = 0$ , and  $\sigma = 1$ .

$$f(z) = \int_0^z \frac{e^{-\frac{x^2}{2}}}{\sqrt{2\pi}} dx = \frac{1}{2} \operatorname{erf}\left(\frac{z}{\sqrt{2}}\right)$$

$$\operatorname{erf}(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-y^2} dy$$

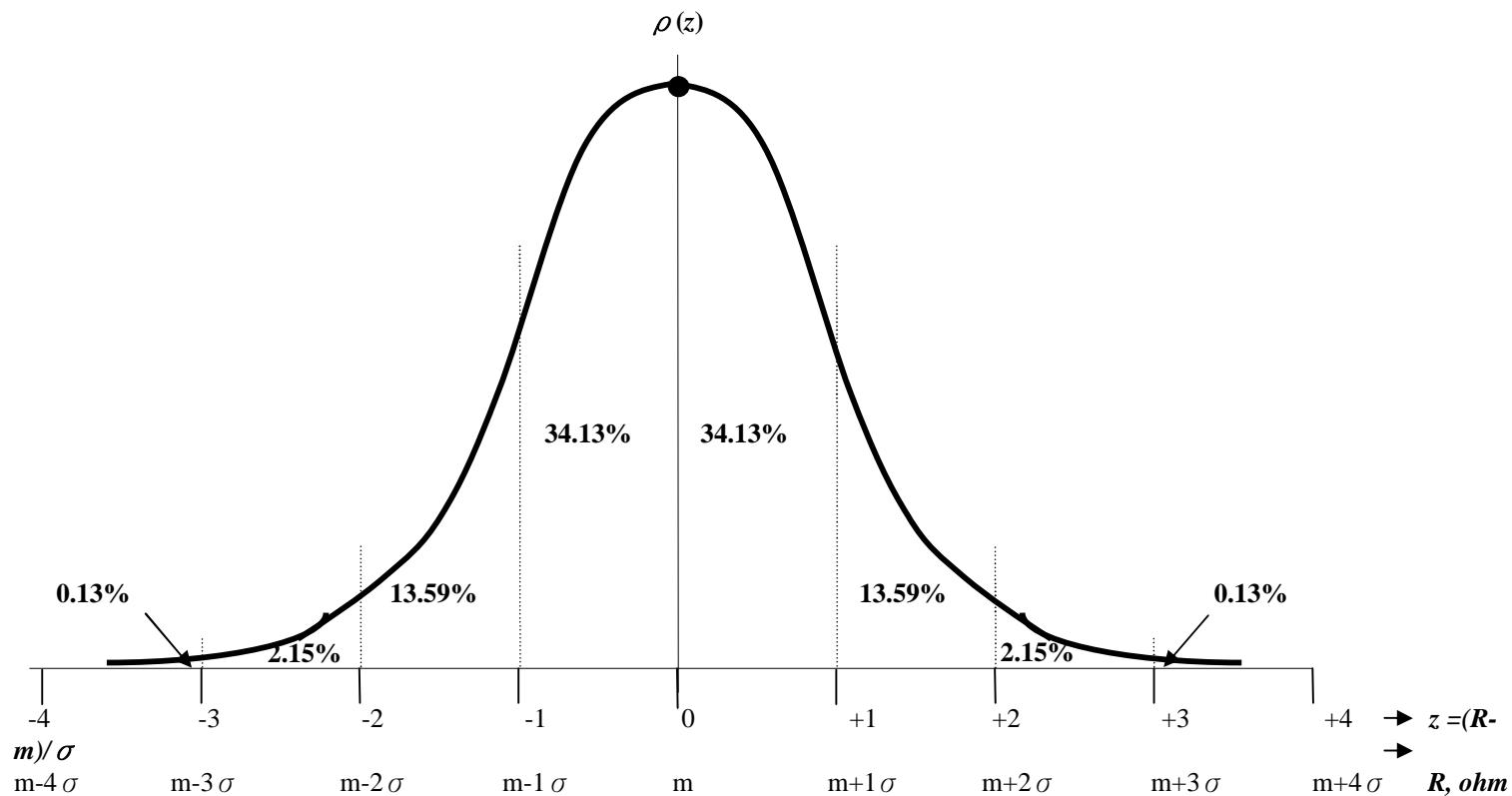


Figure 8.4 At each interval,  $z$ , the appearing percentage of a random variable with a Normal distribution

when the interval is

$-1\sigma < z < +1\sigma$ ,

then the area is  $f(z) = 68.26\%$ ,

when the interval is

$-2\sigma < z < +2\sigma$ ,

then the area is  $f(z) = 95.44\%$ ,

when the interval is

$-3\sigma < z < +3\sigma$ ,

then the area is  $f(z) = 99.74\%$ ,

when the interval is

$z < -3\sigma$ , and  $z > +3\sigma$ ,

then the area is  $f(z) = 0.26\%$ ,

o  $6\sigma$ ,  $C_p$ , and  $C_{pk}$

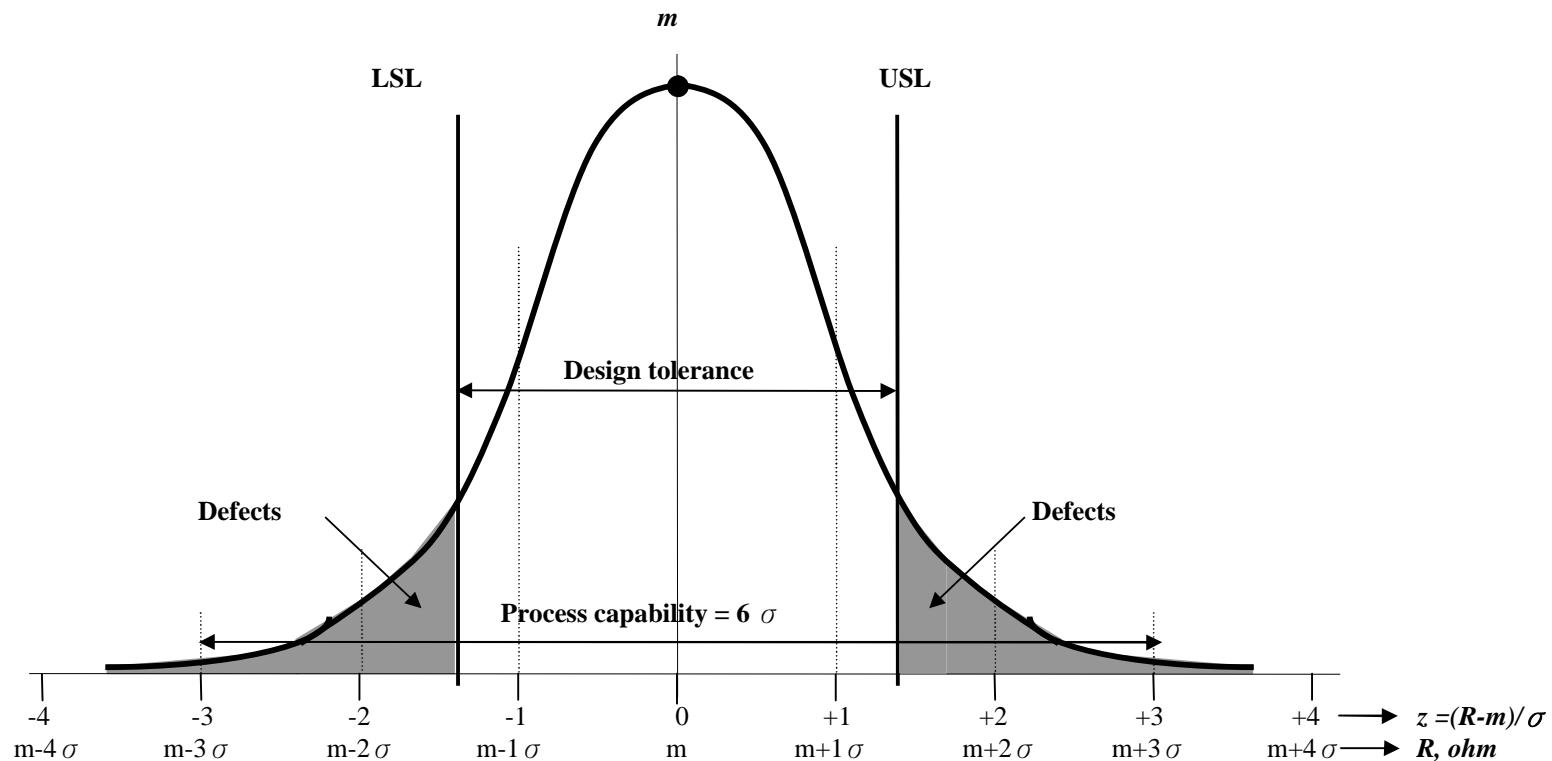


Figure 8.5 The various terminologies of a process with normal distribution

**USL = Upper specification limit,  $\sigma$ ,**  
**LSL = Lower specification limit,  $\sigma$ .**

$$Tolerance = USL - LSL$$

$$Defects = 1 - f(z = USL) - f(z = LSL)$$

where      **USL = Upper specification limit,  $\sigma$ ,**  
                **LSL = Lower specification limit,  $\sigma$ .**

**Capability Index,  $C_p$ , is defined as**

$$C_p = \frac{Design\_Tolerance}{Process\_Capability} \approx \frac{USL - LSL}{6s}$$

**Adjusted Capability Index,  $C_{pk}$ , is defined as**

$$C_{pk} = C_p (1 - K)$$

where      **m = Nominal process mean,  $\sigma$ ,**  
                **m' = Actual process mean,  $\sigma$ .**

$$K = \frac{m - m'}{(USL - LSL)/2}$$

## Example #1

$$Defects = 1 - 2f(z=2s) = 1 - 2 * 47.72\% = 5.56\%$$

$$C_p = \frac{USL - LSL}{6s} = \frac{4s}{6s} = 0.6667 \quad K = \frac{|m - m'|}{(USL - LSL)/2} = 0$$
$$C_{pk} = C_p (1 - K) = 0.6667(1 - 0) = 0.6667$$

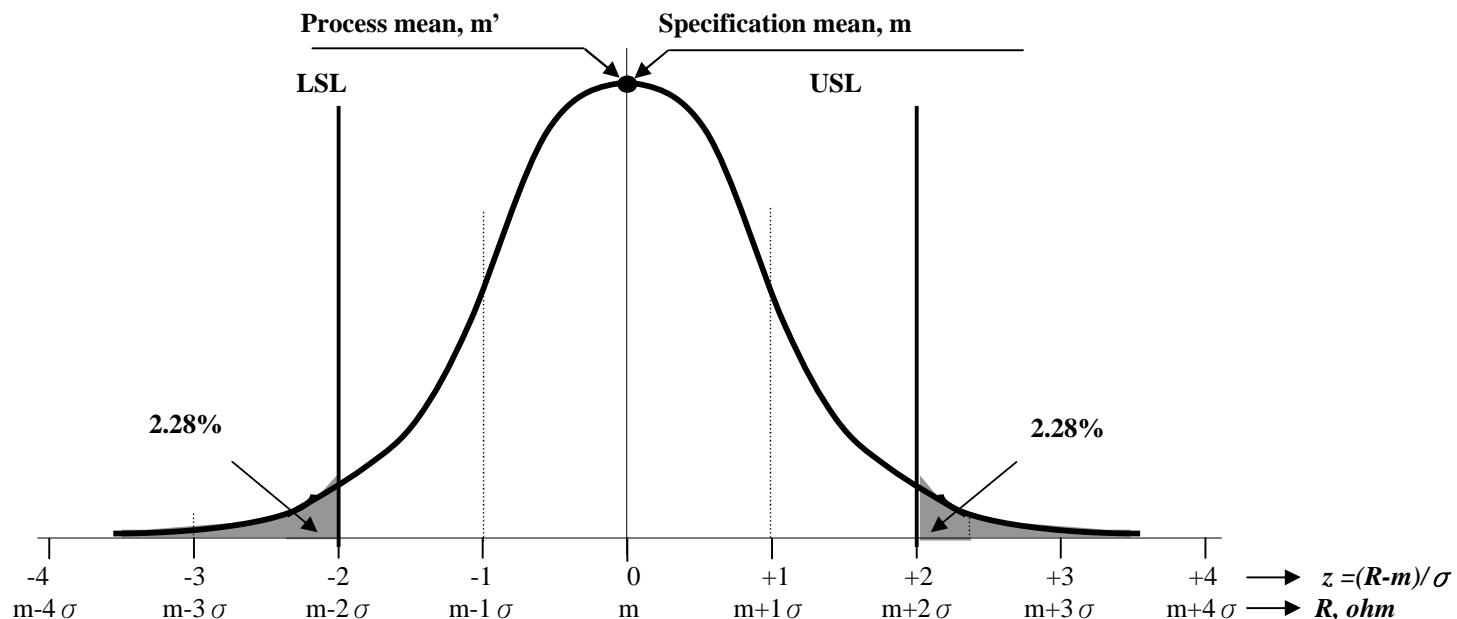


Figure 8.6 A normal distribution with  $m=10$ ,  $\sigma = 0.01$ ,  $USL-LSL=4\sigma$ ,  $m'=m$ .

## Example #2

$$Defects = 1 - 2f(z = 3\sigma) = 1 - 2 * 49.87\% = 0.26\%$$

$$C_p = \frac{USL - LSL}{6\sigma} = \frac{6\sigma}{6\sigma} = 1.0000 \quad K = \frac{|m - m'|}{(USL - LSL)/2} = 0$$

$$C_{pk} = C_p (1 - K) = 1.0000(1 - 0) = 1.0000$$

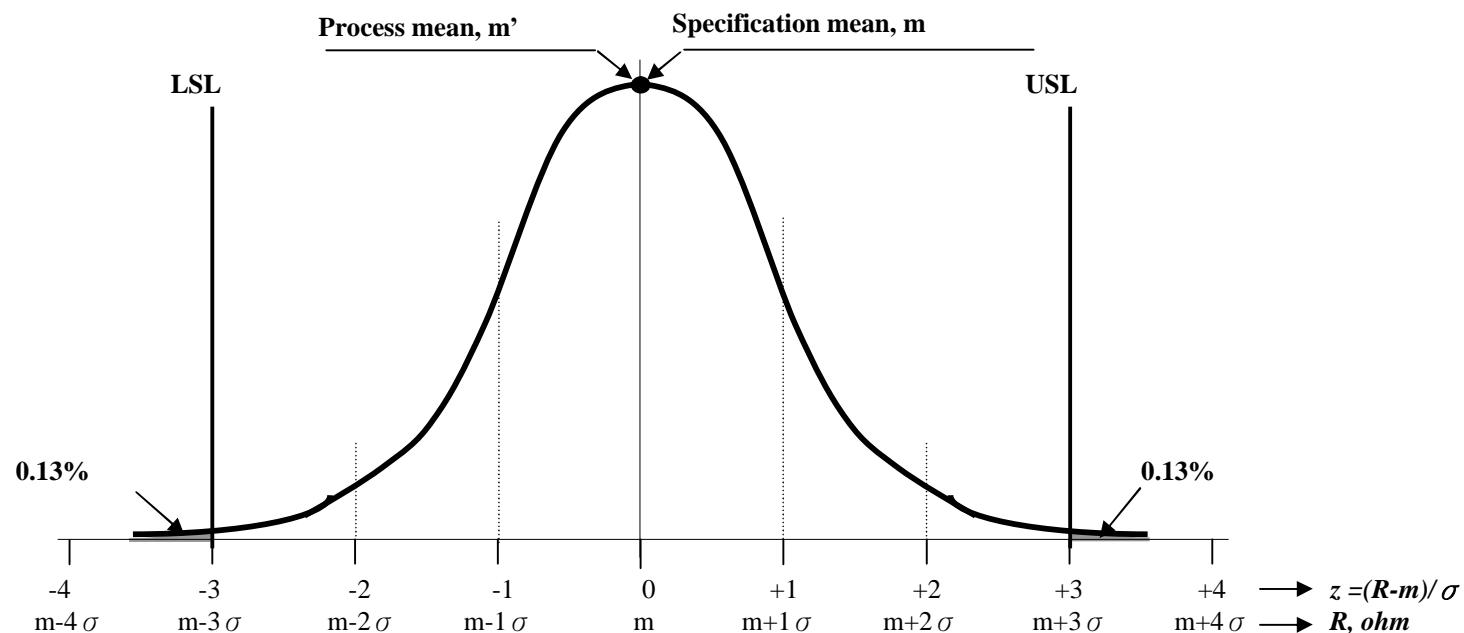


Figure 8.7 A normal distribution with  $m=10$ ,  $\sigma = 0.01$ ,  $USL-LSL=6\sigma$ ,  $m'=m$ .

### Example #3

$$Defects = 1 - f(z=3s) - f(z=-s) = 1 - 34.13\% - 49.87\% = 16\%$$

$$C_p = \frac{USL - LSL}{6s} = \frac{4s}{6s} = 0.6667 \quad K = \frac{|m-m'|}{(USL-LSL)/2} = \frac{1}{4/2} = 0.5000$$

$$C_{pk} = C_p(1-K) = 0.6667(1-0.5) = 0.3334$$

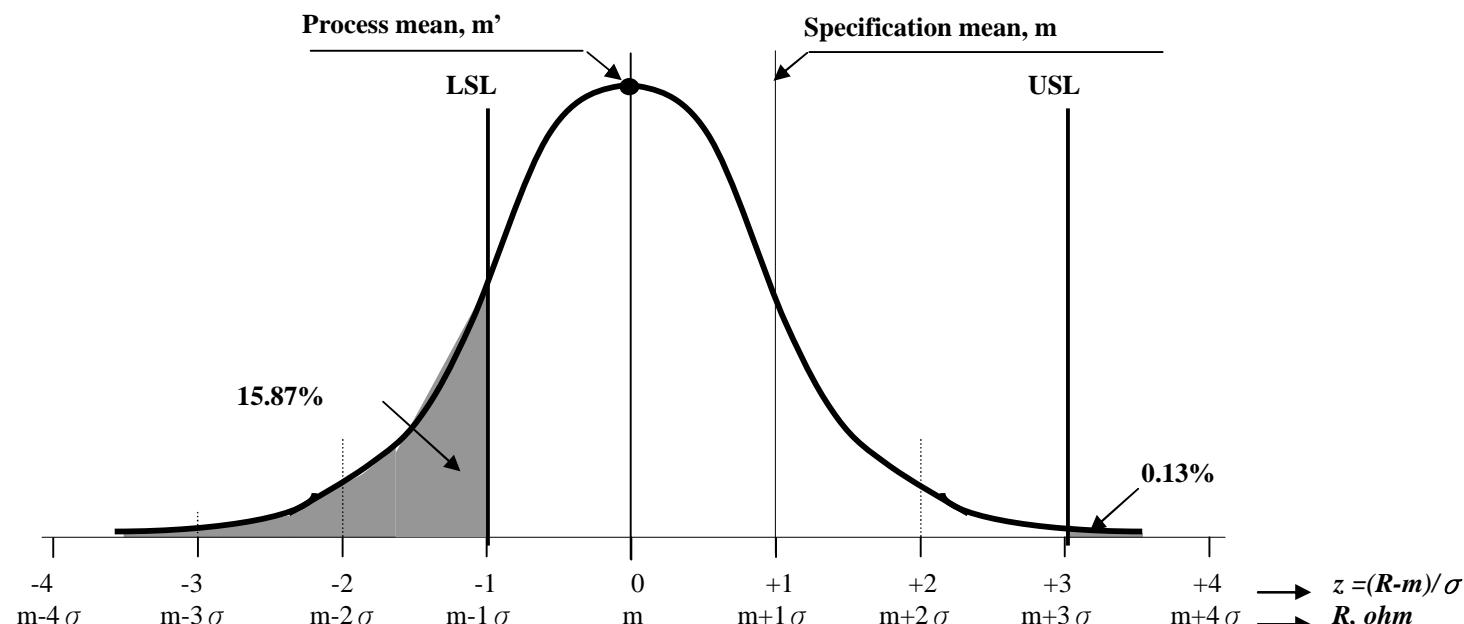


Figure 8.8 A normal distribution with  $m=10$ ,  $\sigma = 0.01$ ,  $USL-LSL=4\sigma$ ,  $m'=9.99$ .

## Example #4

$$Defects = 1 - f(z=0s) - f(z=-4s) = 1 - 0\% - 50\% = 50\%$$

$$C_p = \frac{USL - LSL}{6s} = \frac{4s}{6s} = 0.6667 \quad K = \frac{|m-m'|}{(USL-LSL)/2} = \frac{2}{4/2} = 1$$

$$C_{pk} = C_p (1 - K) = 1.0000 (1 - 1) = 0$$

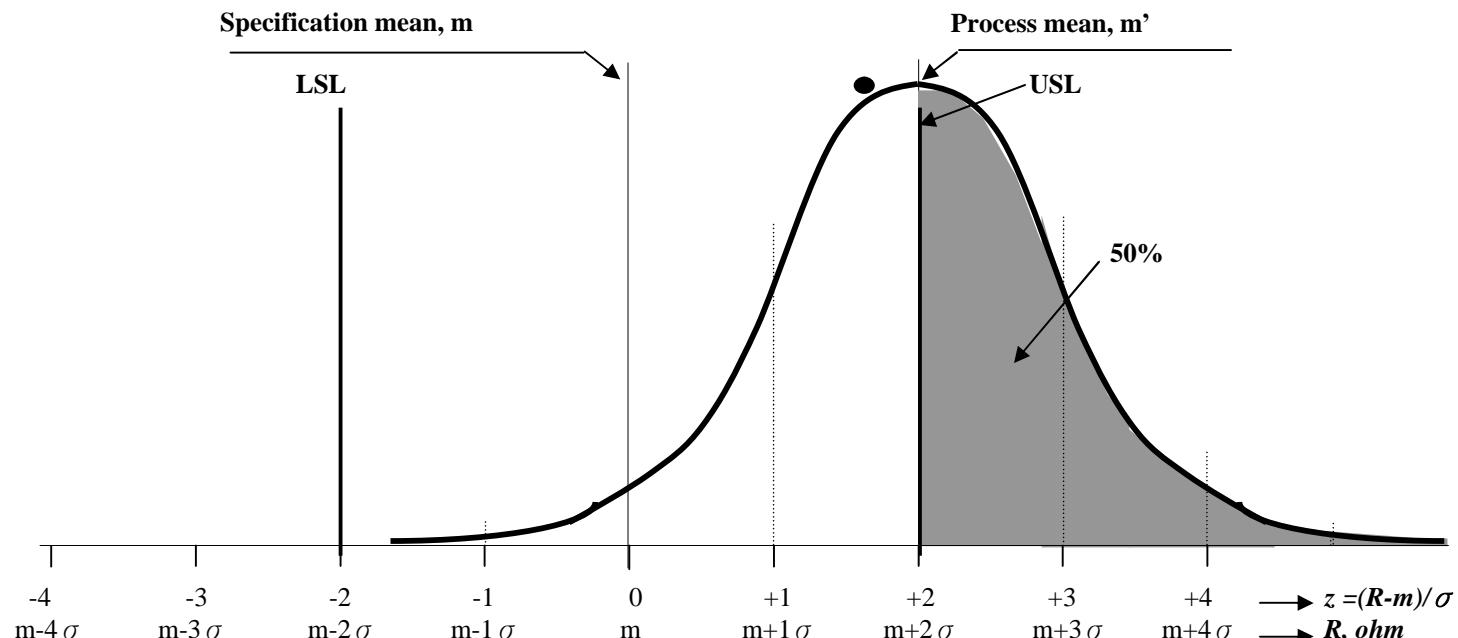


Figure 8.9 A normal distribution with  $m=10$ ,  $\sigma = 0.01$ ,  $USL-LSL=4\sigma$ ,  $m'=10.02$ .

- o Yield rate and DPU

$$DPU = \frac{N_d}{N_p}$$

where       $N_d$  = Number of defects found at all acceptance points,  
 $N_p$  = Number of units processed.

## o Poisson distribution

**Poisson distribution, the occurrence of random defects in manufactured product can be statistically predicted.**

Poisson distribution is a mathematic model to describe the probability distribution of the arrived entities. For instance, in one hour lunch time, say, statistically from 12.00 to 13.00 o'clock, the number of customers getting into a restaurant for lunch. Assuming that the average number of customers is  $\mu$ , and the random number of arrivals at the same time interval is  $x$ , then the probability of the random arrival number,  $P\{x\}$ , is

$$P\{x\} = \frac{\mu^x e^{-\mu}}{x!}$$

$$P\{0\} = \frac{DPU^0 e^{-DPU}}{0!} = e^{-DPU}$$

this is the relationship between the defect-free probability and the average DPU. The first time yield, FTY, can be approximated by the formula:

$$FTY = e^{-DPU}$$

And, in general

$$P\{x\} = \frac{DPU^x e^{-DPU}}{x!}$$

If a process with N steps, 1,2,3,4....N, and the value of DPU in each step is a, b, c, d, .....n respectively. Then, in terms of the formula, the first time yield, FTY, is  $e^{-a}$ ,  $e^{-b}$ ,  $e^{-c}$ ,  $e^{-d}$ ..... $e^{-n}$  correspondingly. The fist time rolled yield for the process is

$$\text{Defect - rate}_{PPM / part} = PPM / part = \frac{DPU}{Parts\_Count}$$

Regardless of process flow or order, the rolled yield can be calculated from the summation of the DPU values in all the steps.

$$FTY_{rolled} = FTY\{A\} * FTY\{B\} * FTY\{C\} * FTY\{D\} ..... * FTY\{N\}$$

$$FTY_{rolled} = e^{-(a + b + c + d + ..... + n)}$$

**Example :**

**Rolled yield for a printed circuit board.**

Assuming that there are totally 3 steps :

Parts placed, parts soldered, and parts assembly.

- a) Part placement = 300 PPM,  
it means 300 parts failed in 1million parts.
- b) Part assembly defect rate = 800 PPM,  
it means 800 assembly-components failed in 1 million parts.
- c) Solder defect rate = 200 PPM,  
it means 200 connected points failed in 1million parts.
- \*) On average, there are 2.3 connections for each part.

Table 8.1 Calculated FTY for a printed circuit board assembly by 3 process steps

# of parts	Parts	Parts	Parts	Total $a+b+c$	Rolled FTY $e^{-(a+b+c)}$
	placement $a$	assembly $b$	soldered $c$		
100	0.030	0.080	0.046	0.156	85.6%
500	0.150	0.400	0.230	0.780	45.8%
1000	0.300	0.800	0.460	1.560	21.0%

## o Approach to $6\sigma$ design and production

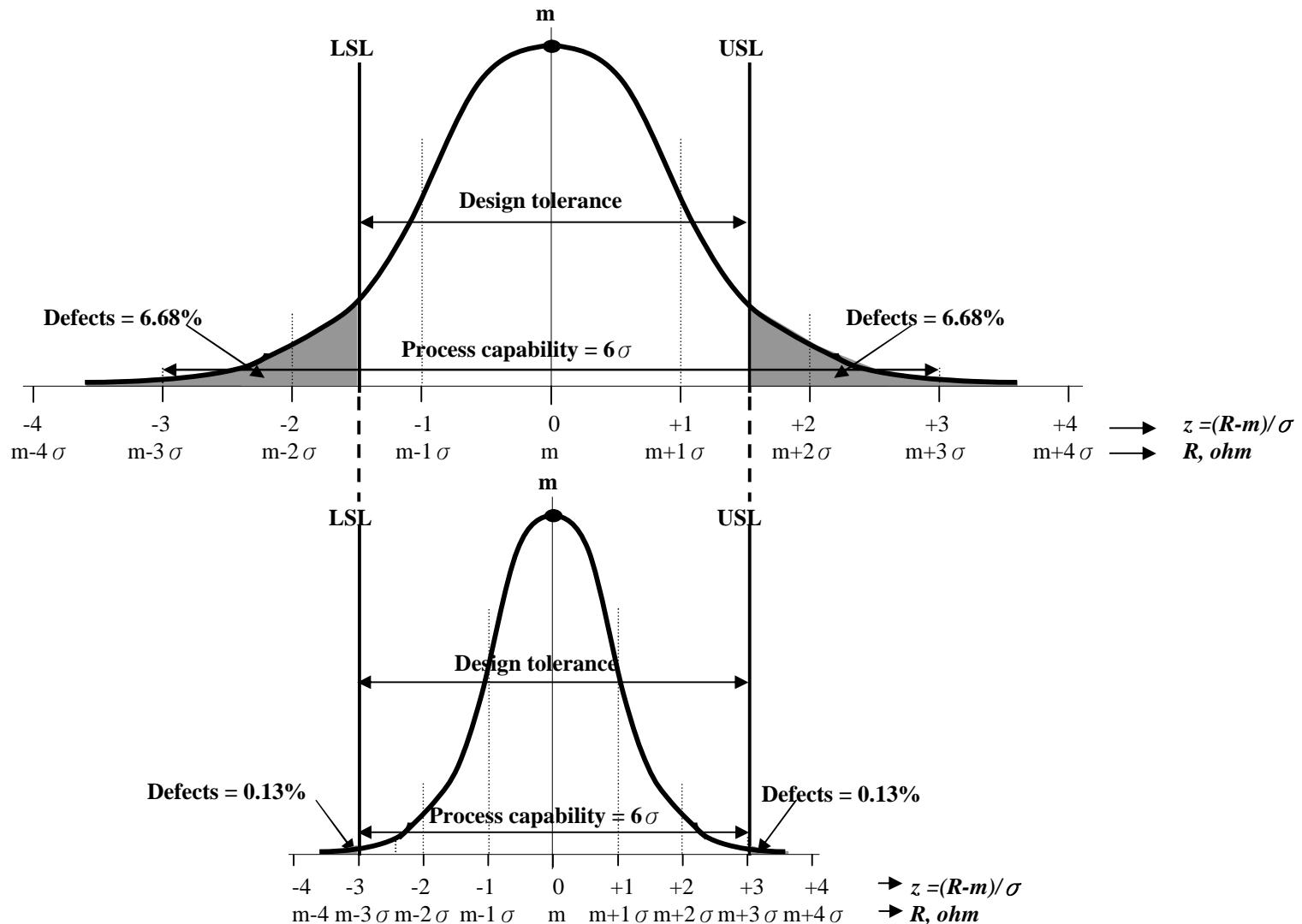


Figure 8.10 Difference of defects when the value of  $\sigma$  is 50% decreased

### 3. Approach to $6\sigma$ design and production

- o Resistor has highest tolerance in IC design

For instance,

$$\frac{\Delta R}{R} \Big|_{R=100\Omega} \Rightarrow \pm 20\%$$

- o Usually, component with higher values has lower relative tolerance.

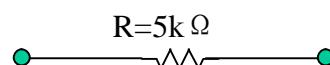
For instance, with the same processing,

$$\frac{\Delta R}{R} \Big|_{R=10k\Omega} = \frac{1}{2} \frac{\Delta R}{R} \Big|_{R=5k\Omega}$$

## o Resistors in parallel

To build a  $5\text{k}\Omega$  resistor

by  $5\text{k}\Omega$  resistor



by  $10\text{k}\Omega$  resistors

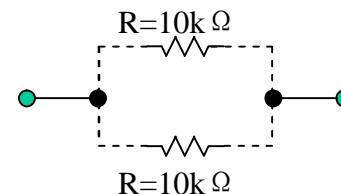


Figure 8.11 A  $5\text{k}\Omega$  resistor is replaced by two  $10\text{k}\Omega$  resistors in parallel

$$R_{t1} = R \Big|_{R=5\text{k}\Omega}$$

$$R_{t2} = \frac{RR}{R+R} = \frac{R}{2} \Big|_{R=10\text{k}\Omega}$$

$$\frac{\Delta R_{t1}}{R_{t1}} = \frac{\Delta R}{R} \Big|_{R=5\text{k}\Omega}$$

$$\frac{\Delta R_{t2}}{R_{t2}} = \frac{\Delta R}{R} \Big|_{R=10\text{k}\Omega}$$

If  $\frac{\Delta R}{R} \Big|_{R=5\text{k}\Omega} = 2 \frac{\Delta R}{R} \Big|_{R=10\text{k}\Omega}$

Then,  $\frac{\Delta R_{t2}}{R_{t2}} = \frac{1}{2} \frac{\Delta R_{t1}}{R_{t1}}$

## o Capacitors in series

To build a 5pF capacitor

by 5pF capacitor



by 10pF capacitors

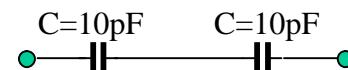


Figure 8.12 A 5 pF capacitor is replaced by two 10 pF capacitors in series

$$C_{t1} = C \Big|_{C=5 \text{ pF}}$$

$$C_{t2} = \frac{CC}{C+C} = \frac{C}{2} \Big|_{C=10 \text{ pF}}$$

$$\frac{\Delta C_{t1}}{C_{t1}} = \frac{\Delta C}{C} \Big|_{C=5 \text{ pF}}$$

$$\frac{\Delta C_{t2}}{C_{t2}} = \frac{\Delta C}{C} \Big|_{C=10 \text{ pF}}$$

If  $\frac{\Delta C}{C} \Big|_{C=5 \text{ pF}} = 2 \frac{\Delta C}{C} \Big|_{C=10 \text{ pF}}$

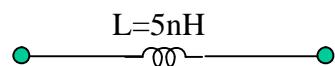
Then,

$$\frac{\Delta C_{t2}}{C_{t2}} = \frac{1}{2} \frac{\Delta C_{t1}}{C_{t1}}$$

## o Inductors in parallel

To build a 5nH inductortor

by 5nH inductortor



by 10nH inductors

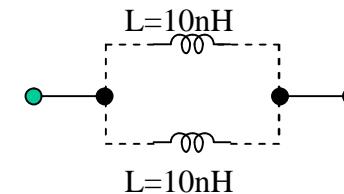


Figure 8.13 A 5 nH inductor is replaced by two 10 nH inductors in series

$$L_{t1} = L \Big|_{L=5 \text{ nH}}$$

$$L_{t2} = \frac{LL}{L+L} = \frac{L}{2} \Big|_{L=10 \text{ nH}}$$

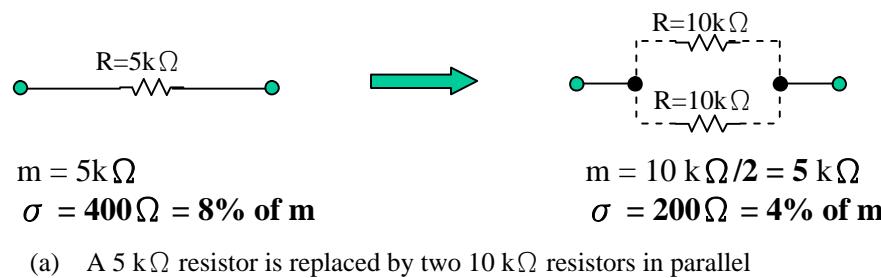
$$\frac{\Delta L_{t1}}{L_{t1}} = \frac{\Delta L}{L} \Big|_{L=5 \text{ nH}}$$

$$\frac{\Delta L_{t2}}{L_{t2}} = \frac{\Delta L}{L} \Big|_{L=10 \text{ nH}}$$

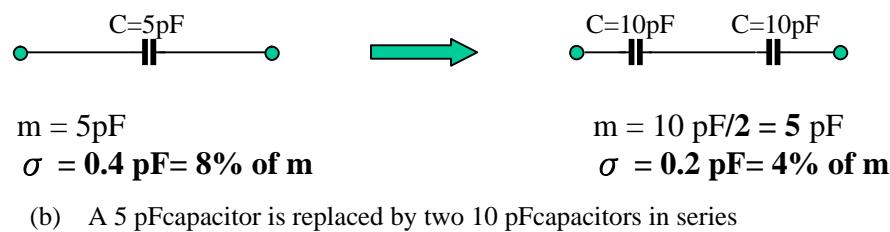
If  $\frac{\Delta L}{L} \Big|_{L=5 \text{ nH}} = 2 \frac{\Delta L}{L} \Big|_{L=10 \text{ nH}}$

Then,  $\frac{\Delta L_{t2}}{L_{t2}} = \frac{1}{2} \frac{\Delta L_{t1}}{L_{t1}}$

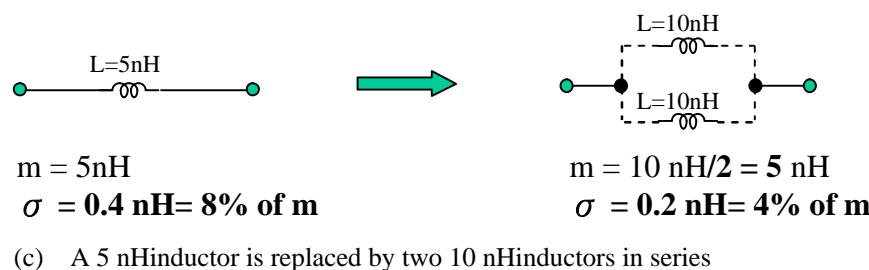
Usually it does not reduce the tolerance by the way of inductors in parallel because it is too expensive !



(a) A  $5\text{k}\Omega$  resistor is replaced by two  $10\text{k}\Omega$  resistors in parallel



(b) A  $5\text{pF}$  capacitor is replaced by two  $10\text{pF}$  capacitors in series

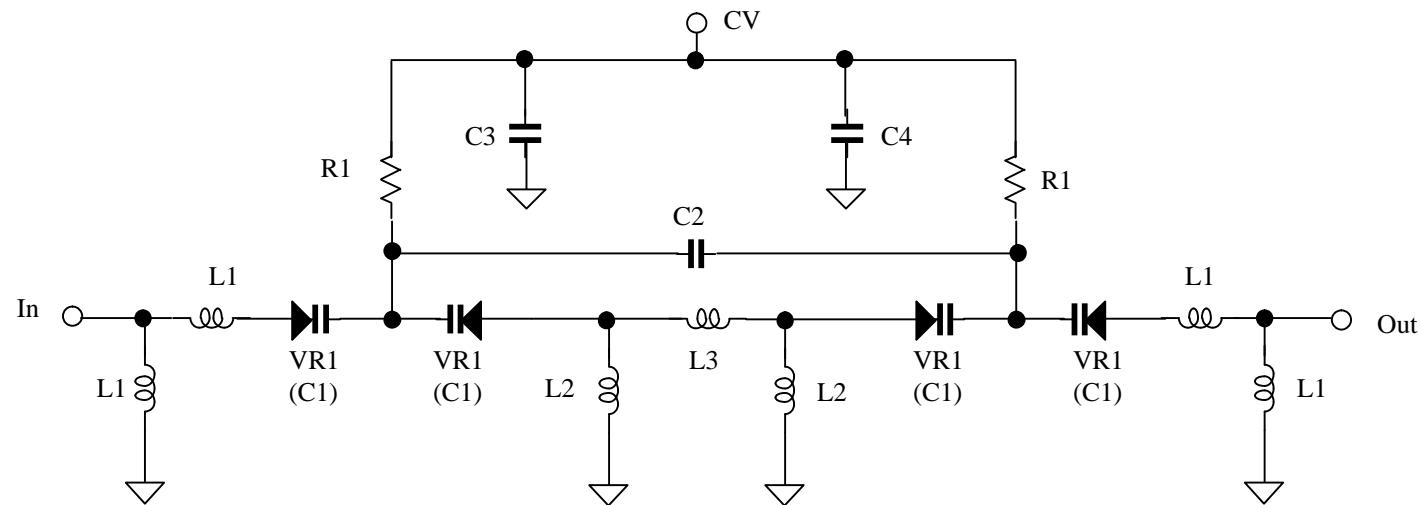


(c) A  $5\text{nH}$  inductor is replaced by two  $10\text{nH}$  inductors in series

Figure 8.14 Variation of  $\sigma$  in the various replacements

## 4. An example : Tunable filter design

### o Schematic of a tunable filter



L1 : Inductor 4.5 nH// 27 k  $\Omega$  // 0.2 pF

L2 : Inductor 8.8 nH// 27 k  $\Omega$  // 0.2 pF

L3 : Inductor 40.5 nH// 27 k  $\Omega$  // 0.2 pF

C1 : Capacitance of varactor 13.75 pF when CV=5v

C2 : Capacitor 2.4 pF

C3 : Capacitor 100 pF

C4 : Capacitor 10000 pF

R1 : Resistor 20 k $\Omega$

CV : 5 v

Figure 8.15 Schematic of a UHF tunable filter



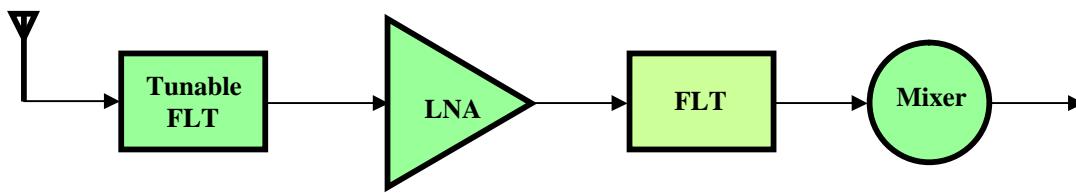
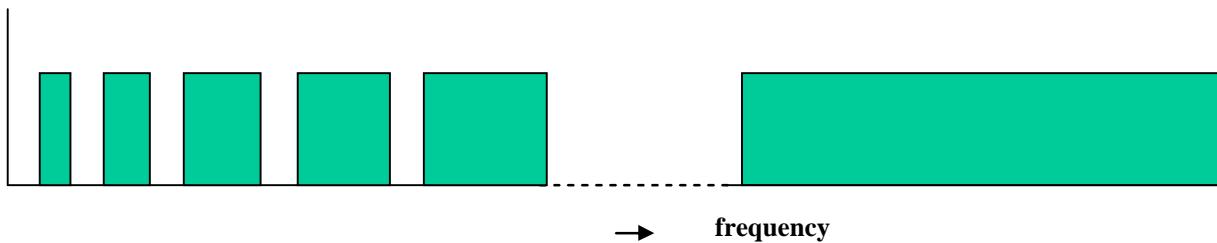
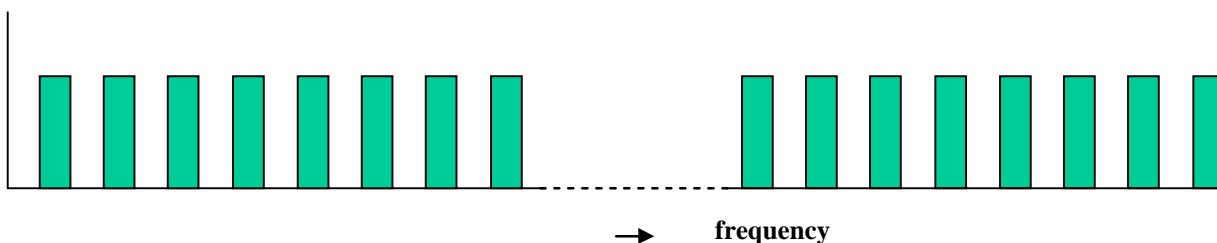


Figure 8.15a A tunable filter is added in the front end of the receiver for better selectivity



(a) Popular cases : Bandwidth is changed as the frequency response is moved



(b) Ideal cases : Bandwidth is kept unchanged as the frequency response is moved

Figure 8.15b Frequency response of a tunable filter moved from low end to high end as the control voltage is increased

## **o Main coupling : Inductive coupling**

- \* An improper coupling unable a tunable filter tuned over a wide frequency tuning range .
- \* In the case of capacitor coupling,

$$Q = \omega_0 / (BW) = 1 / (2RC \omega_0)$$

$$BW = 2RC\omega_0^2$$

$$\partial (BW) / \partial (\omega_0) = 4RC\omega_0$$

- \* In the case of inductor coupling,

$$Q = \omega_0 / (BW) = L\omega_0 / (2R)$$

$$BW = 2R / L$$

$$\partial (BW) / \partial (\omega_0) = 0$$

<b>where</b>	<b>Q</b>	= Quality factor of filter ;
	<b>ω₀</b>	= Tuned central frequency ;
	<b>BW</b>	= Bandwidth @ ω₀;
	<b>L</b>	= Inductance of coupling inductor ;
	<b>R</b>	= Equivalent resonant resistance of tank circuit @ ω₀.

**From the above expressions , it is concluded that**

- 1) **In the case of inductor-coupling, the bandwidth of the filter is a constant or independent of the tuning frequency, while**
- 2) **In the case of capacitor-coupling, the bandwidth of the filter is a function or dependent of the tuning frequency. It is increased as the tuning frequency is increased.**

**Consequently,**

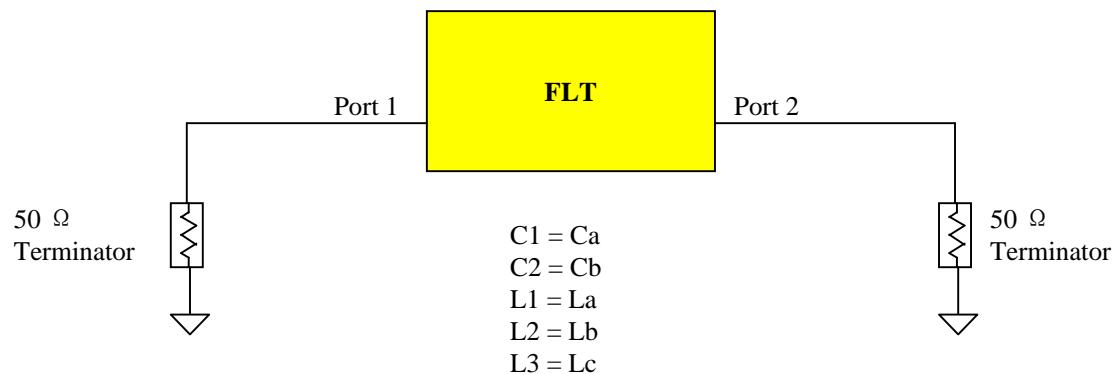
**The bandwidth could be kept in an almost constant for a wide tuning frequency range if the coupling element is only an inductor.**

**It is therefore decided to use an inductor as the primary coupling element between the 2 tank circuits, which is L3 as shown above.**

## **o Second coupling : Capacitive coupling**

- \* The capacitor, C2, is the second coupling component between the two tank circuits;
- \* It forms a “zero” at the imaginary frequency;
- \* This “zero” traces the central frequency,  $\omega_0$ , over a wide frequency tuning range.

## o Monte Carlo Analysis



Equation  $C_a = \text{RandvarGaussian}, 13.75 \text{ pF} \pm 5\%$

Equation  $C_b = \text{RandvarGaussian}, 2.4 \text{ pF} \pm 5\%$

Equation  $L_a = \text{RandvarGaussian}, 4.5 \text{ nH} \pm 7\%$

Equation  $L_b = \text{RandvarGaussian}, 8.8 \text{ nH} \pm 7\%$

Equation  $L_c = \text{RandvarGaussian}, 40.5 \text{ nH} \pm 7\%$

Figure 8.16 Simulation page for Monte-Carlo analysis  
(Strictly speaking, it is not a Gaussian but a normal distribution here.)

\* Frequency response without tolerance

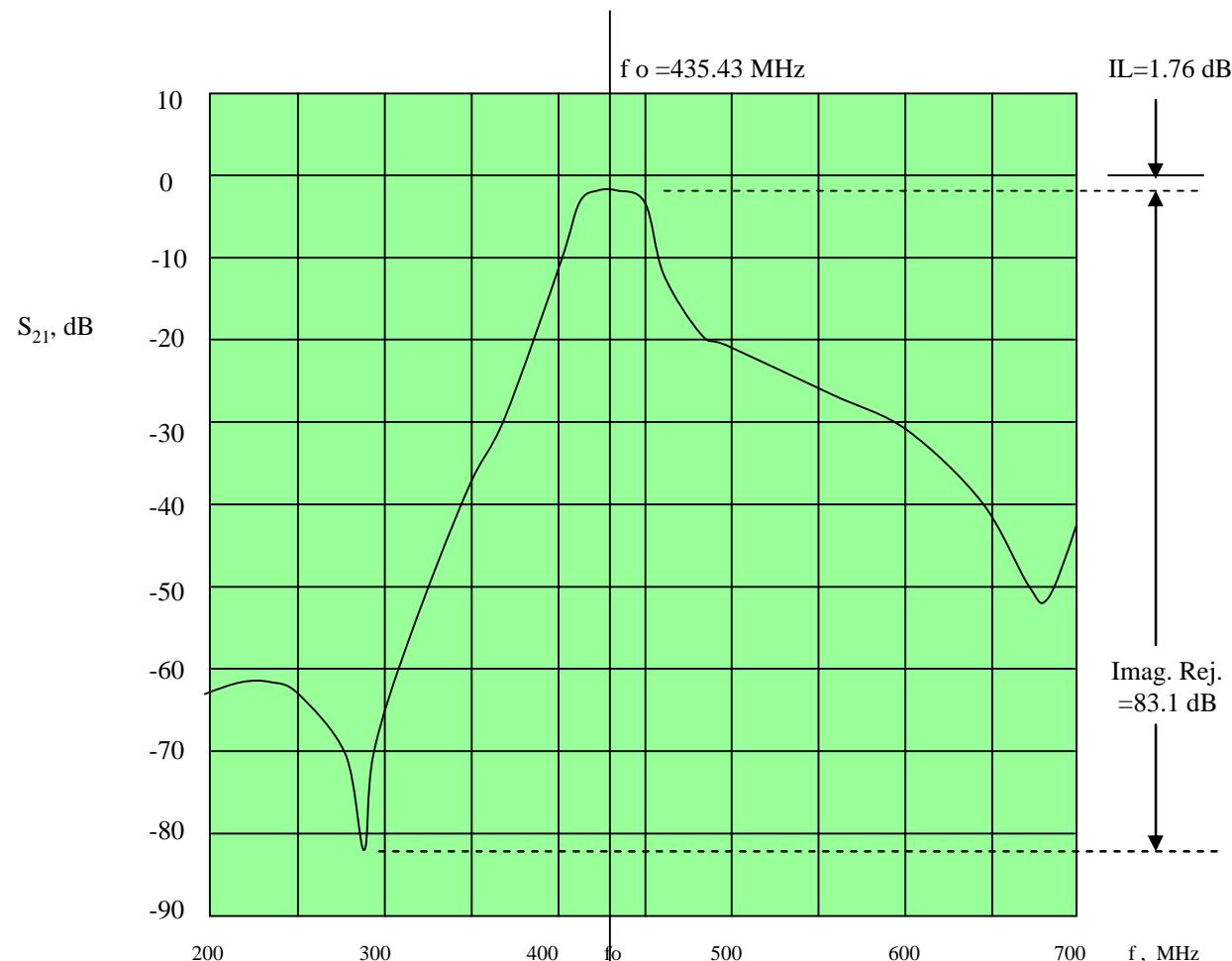


Figure 8.17 Typical frequency response of tunable filter without tolerance

\* Case #3 : Bandwidth is too narrow

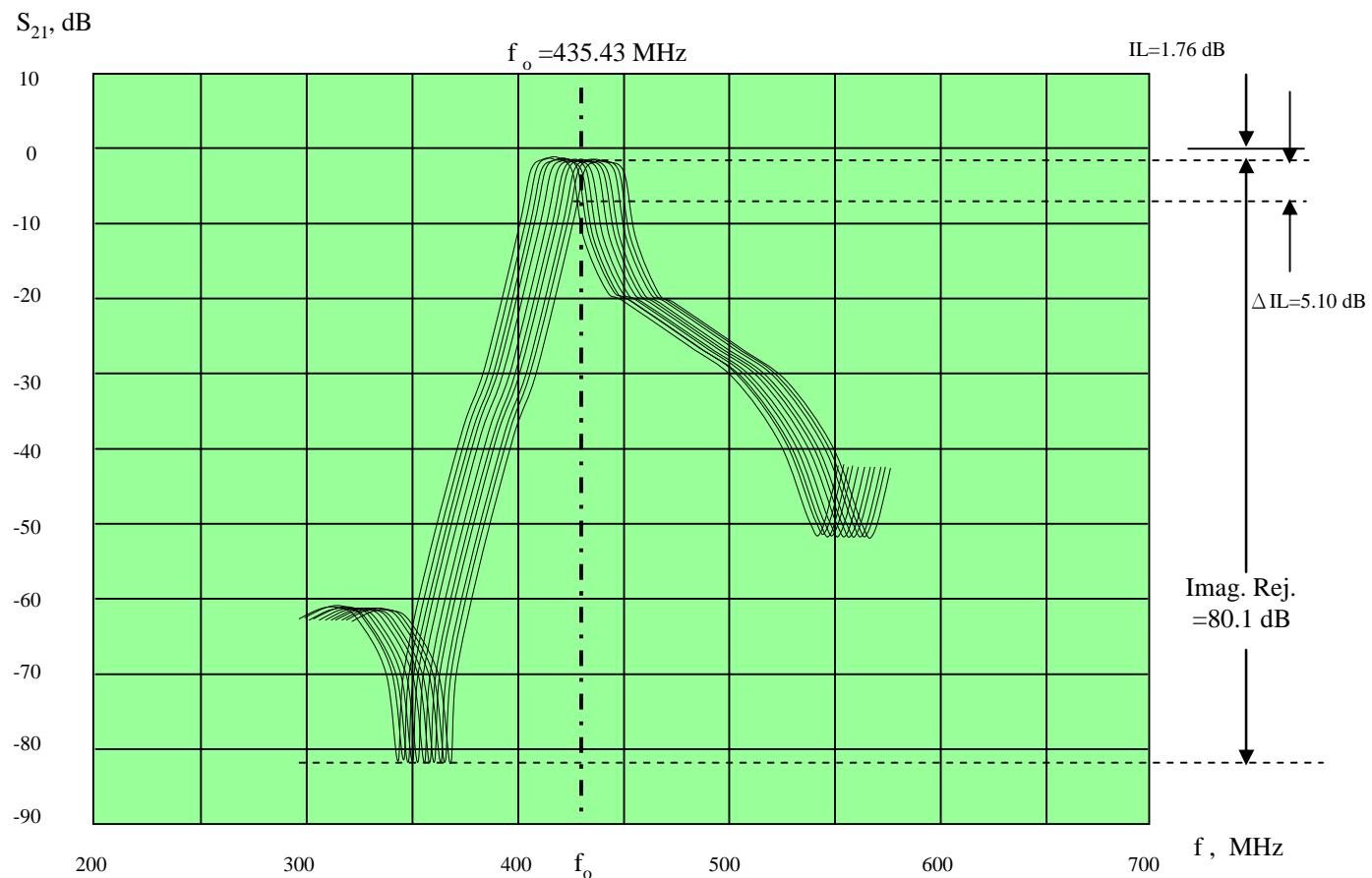


Figure 8.18 Frequency response of tunable filter with tolerance  
---Bandwidth is too narrow

\* Case #2 : Bandwidth is appropriate

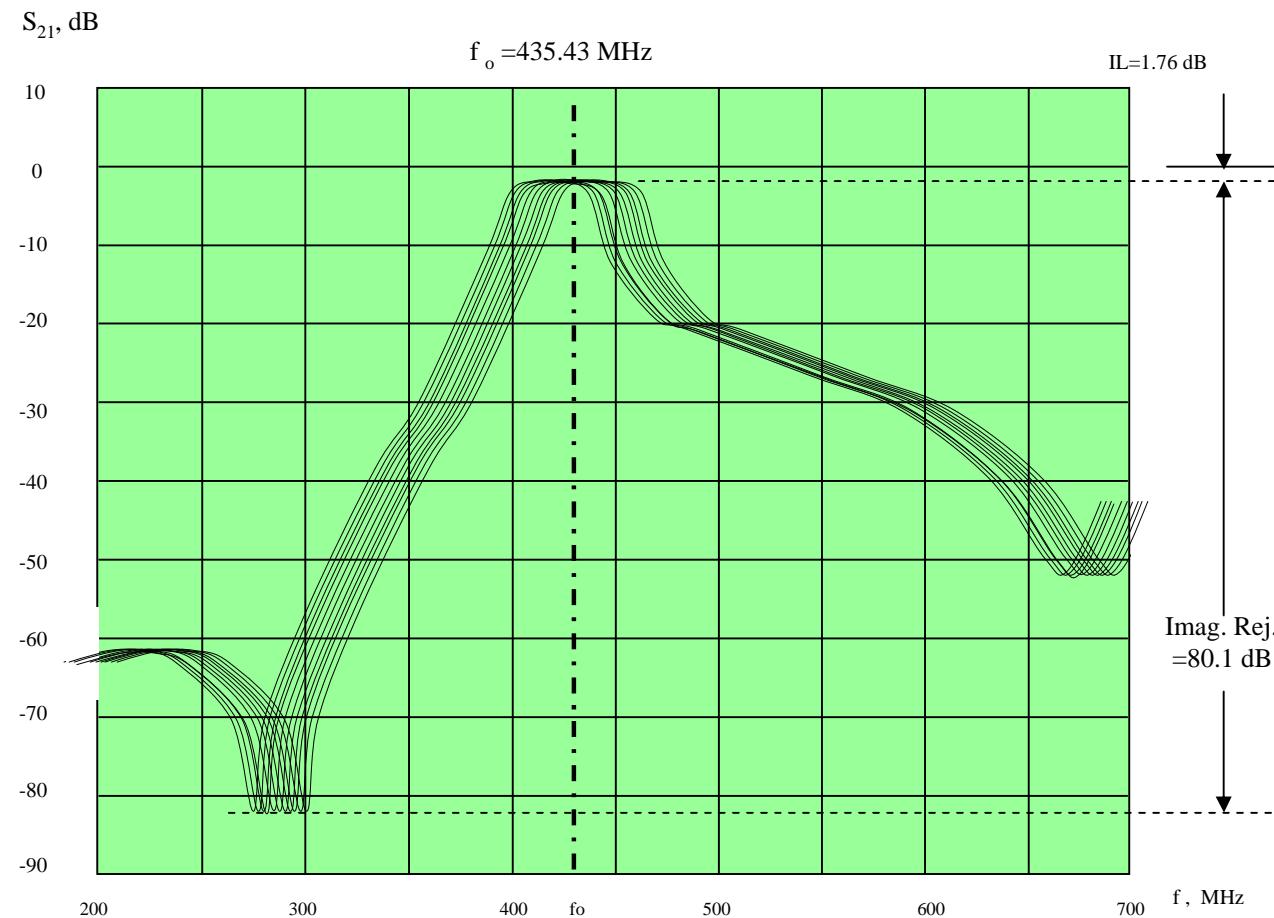


Figure 8.19 Frequency response of tunable filter with tolerance  
---Bandwidth is appropriate

\* Case #1 : Bandwidth is too wide

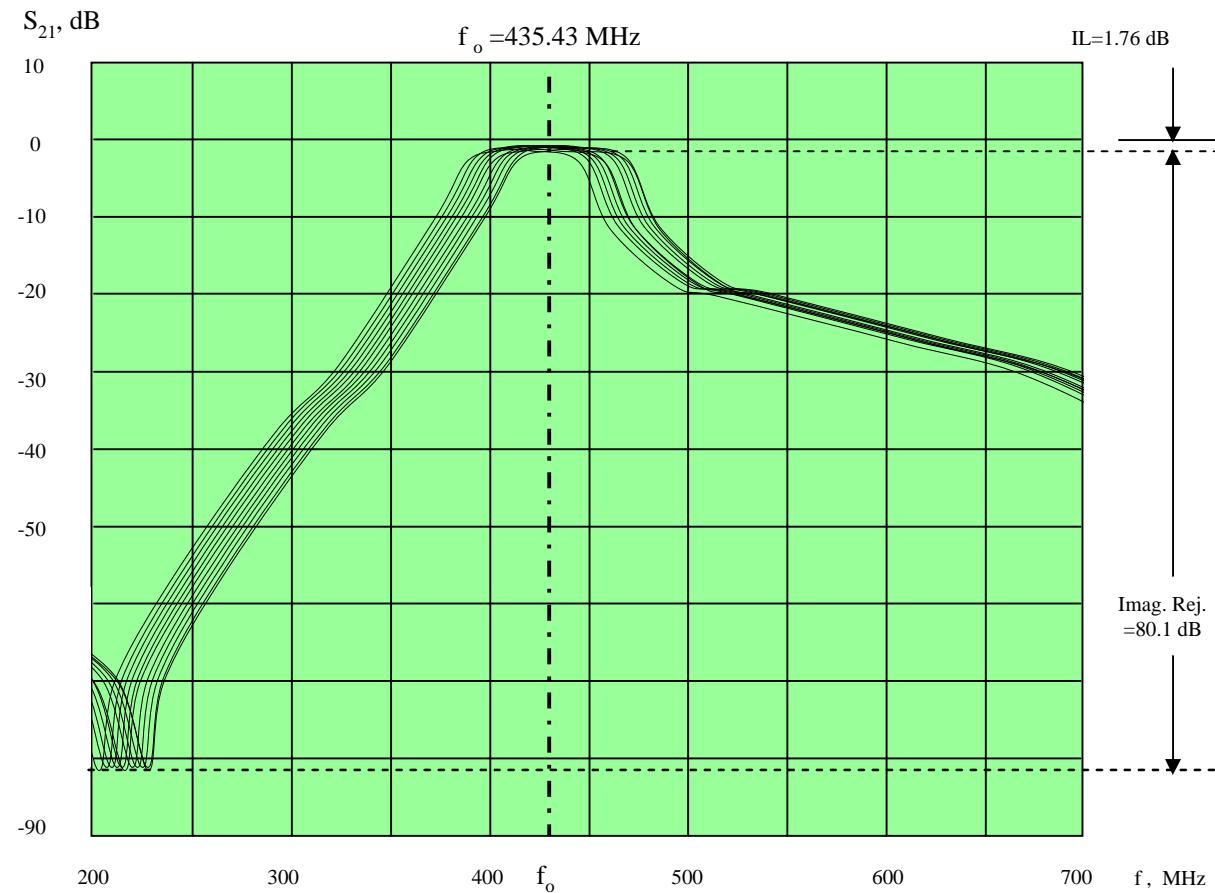


Figure 8.20 Frequency response of tunable filter with tolerance  
---Bandwidth is too wide

\* Yield rate & its histogram of IL less than 2.5 dB ( For case #2)

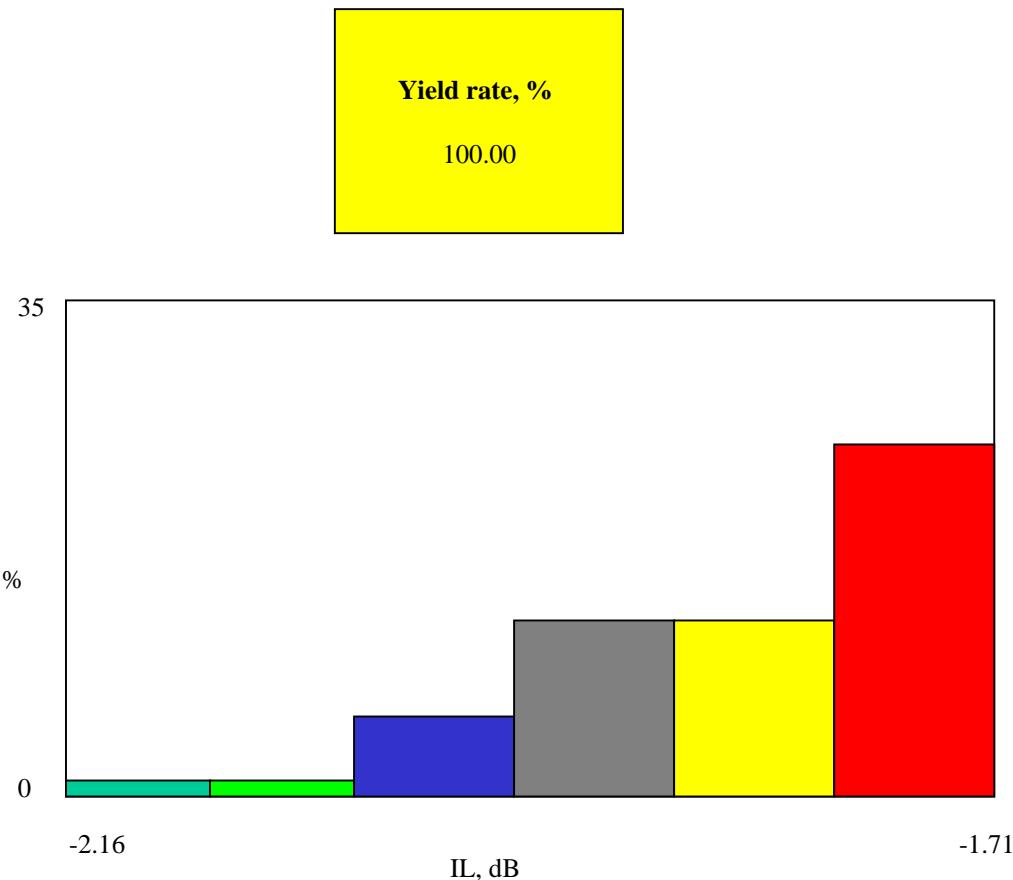
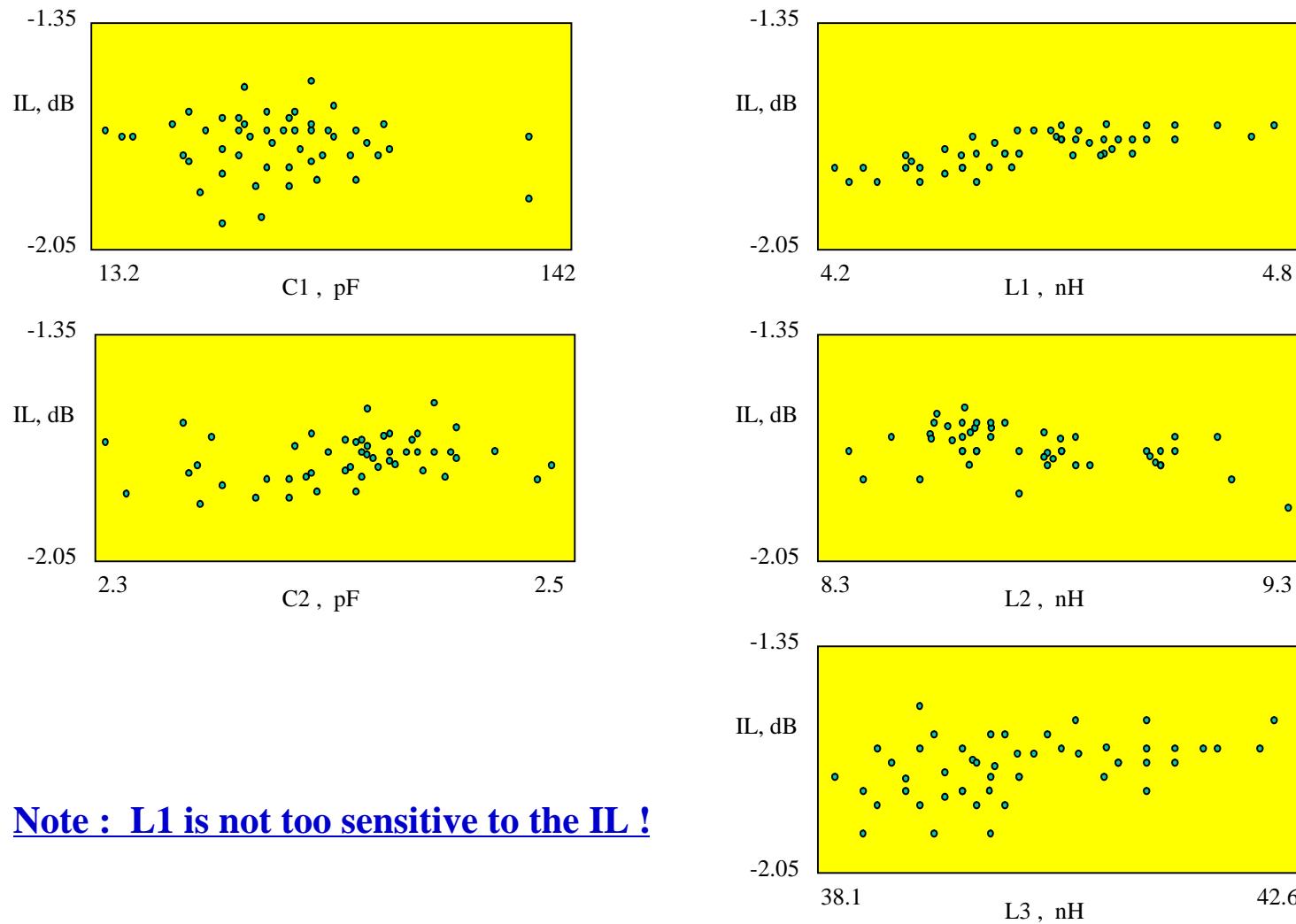


Figure 8.21 Display of insertion loss histogram and yield rate for  $IL < 2.5 dB$

\* IL performance of parts with tolerance ( For case #2 )



Note : L1 is not too sensitive to the IL !

Figure 8.22 The effect of individual part's value on the insertion loss

- \* Yield rate & its histogram of Imag.Rej. greater than 60 dB ( For case #2 )

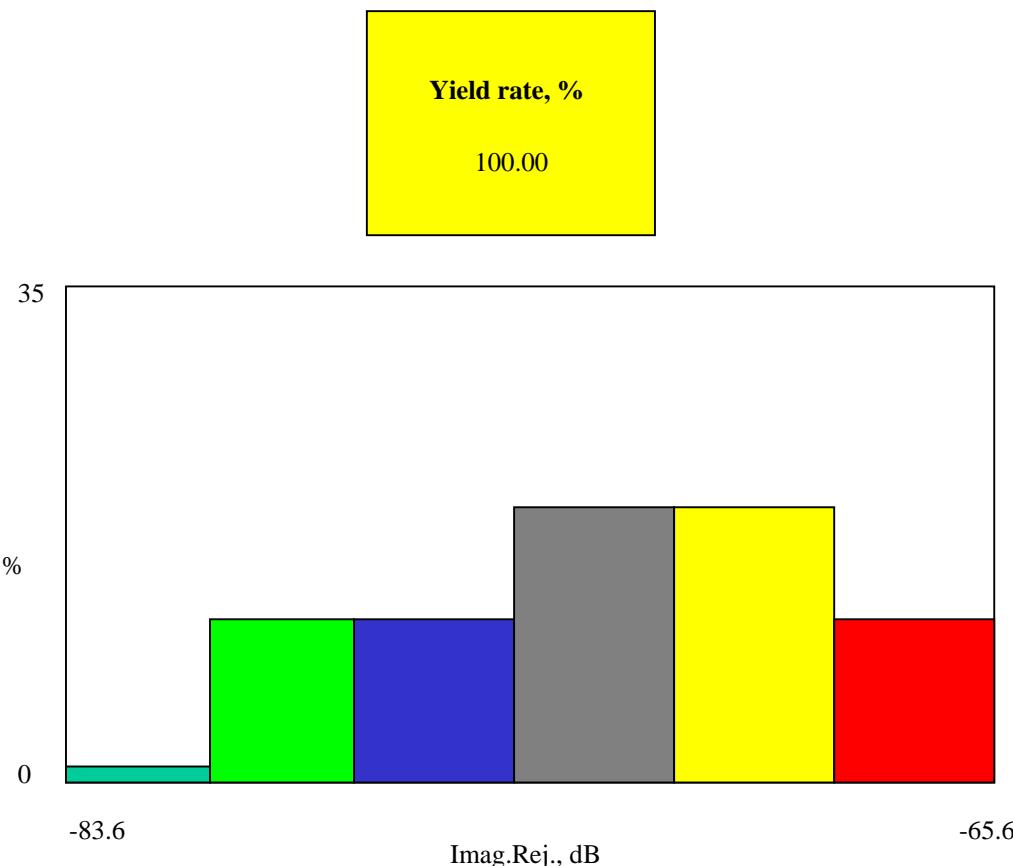
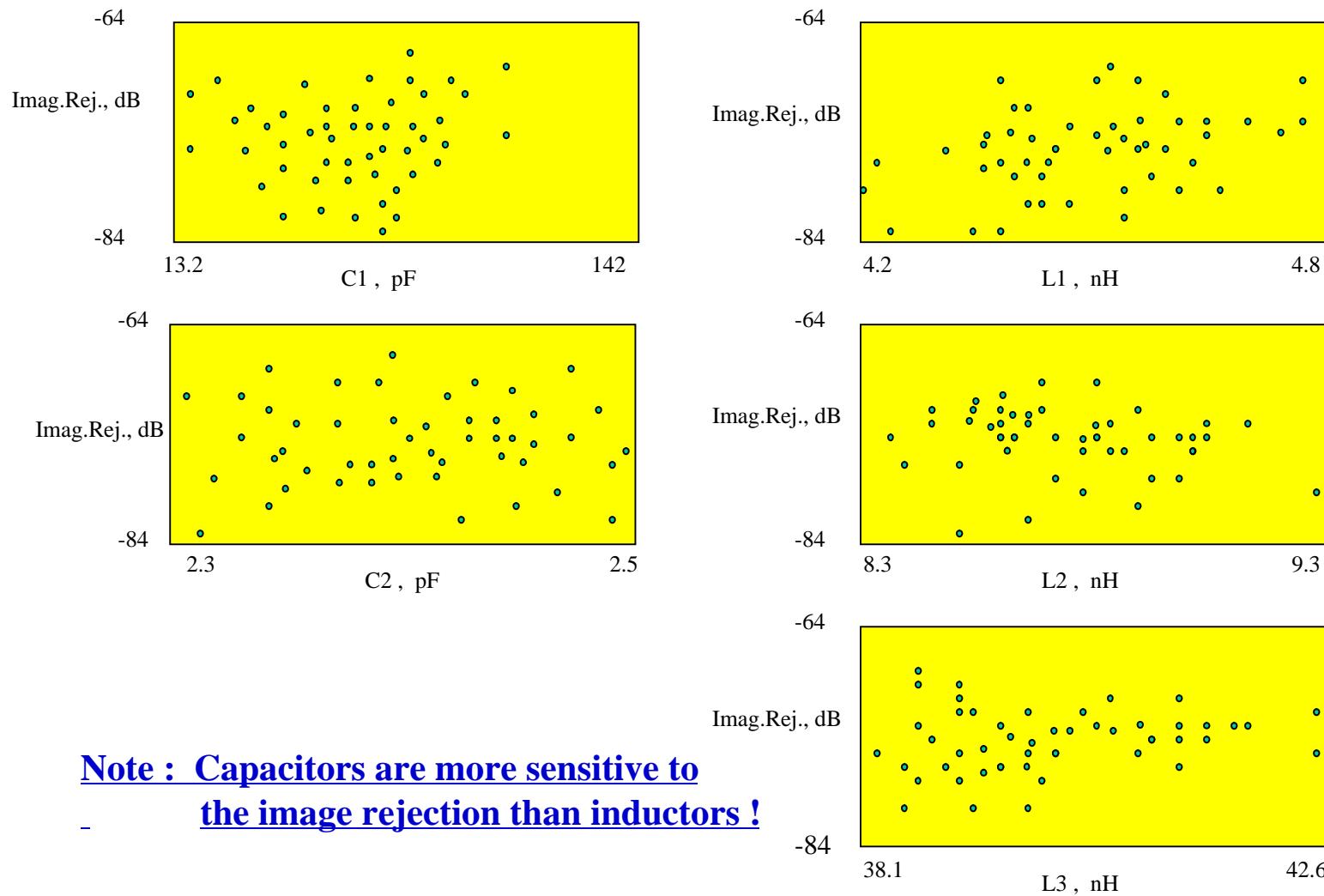


Figure 8.23 Display of image rejection histogram and yield rate for IR>60dB

\* Image Rejection performance of parts with tolerance ( For case #2 )



Note : Capacitors are more sensitive to  
the image rejection than inductors !

Figure 8.24 The effect of individual part's value on the image rejection

## 5.Appendix: Table of the normal distribution

Table 8.2 Normal distribution

<b>Z</b>	<b>0</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>
<b>0.0</b>	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
<b>0.1</b>	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0754
<b>0.2</b>	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
<b>0.3</b>	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
<b>0.4</b>	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
<b>0.5</b>	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
<b>0.6</b>	.2258	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2518	.2549
<b>0.7</b>	.2580	.2612	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
<b>0.8</b>	.2881	.2910	.2939	.2967	.2996	.3023	.3051	.3078	.3016	.3133
<b>0.9</b>	.3135	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
<b>1.0</b>	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
<b>1.1</b>	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
<b>1.2</b>	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
<b>1.3</b>	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
<b>1.4</b>	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
<b>1.5</b>	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
<b>1.6</b>	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
<b>1.7</b>	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
<b>1.8</b>	.4641	.4649	.4656	.4664	.4671	.4678	.46	.4693	.4699	.4706
<b>1.9</b>	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767

<b>Z</b>	<b>0</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>
<b>2.0</b>	.4772	.4778	.4783	.4778	.4793	.4798	.4803	.4808	.4812	.4817
<b>2.1</b>	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
<b>2.2</b>	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
<b>2.3</b>	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
<b>2.4</b>	.4918	.4920	.4922	.4925	.4925	.4929	.4931	.4932	.4934	.4936
<b>2.5</b>	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
<b>2.6</b>	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
<b>2.7</b>	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
<b>2.8</b>	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
<b>2.9</b>	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
<b>3.0</b>	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990
<b>3.1</b>	.4990	.4991	.4991	.4991	.4992	.4992	.4992	.4992	.4993	.4993
<b>3.2</b>	.4993	.4993	.4994	.4994	.4994	.4994	.4994	.4995	.4995	.4995
<b>3.3</b>	.4995	.4995	.4995	.4996	.4996	.4996	.4996	.4996	.4996	.4997
<b>3.4</b>	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4997	.4998
<b>3.5</b>	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998
<b>3.6</b>	.4998	.4998	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999
<b>3.7</b>	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999
<b>3.8</b>	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999
<b>3.9</b>	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000

$$f(z) = \int_0^z \frac{e^{-\frac{x^2}{2}}}{\sqrt{2\pi}} dx = \frac{1}{2} \operatorname{erf}\left(\frac{z}{\sqrt{2}}\right)$$

## 射 频 和 天 线 设 计 培 训 课 程 推 荐

易迪拓培训([www.edatop.com](http://www.edatop.com))由数名来自于研发第一线的资深工程师发起成立，致力并专注于微波、射频、天线设计研发人才的培养；我们于 2006 年整合合并微波 EDA 网([www.mweda.com](http://www.mweda.com))，现已发展成为国内最大的微波射频和天线设计人才培养基地，成功推出多套微波射频以及天线设计经典培训课程和 ADS、HFSS 等专业软件使用培训课程，广受客户好评；并先后与人民邮电出版社、电子工业出版社合作出版了多本专业图书，帮助数万名工程师提升了专业技术能力。客户遍布中兴通讯、研通高频、埃威航电、国人通信等多家国内知名公司，以及台湾工业技术研究院、永业科技、全一电子等多家台湾地区企业。

易迪拓培训课程列表：<http://www.edatop.com/peixun/rfe/129.html>

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### 射频工程师养成培训课程套装

该套装精选了射频专业基础培训课程、射频仿真设计培训课程和射频电路测量培训课程三个类别共 30 门视频培训课程和 3 本图书教材；旨在引领学员全面学习一个射频工程师需要熟悉、理解和掌握的专业知识和研发设计能力。通过套装的学习，能够让学员完全达到和胜任一个合格的射频工程师的要求…

课程网址：<http://www.edatop.com/peixun/rfe/110.html>

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### ADS 学习培训课程套装

该套装是迄今国内最全面、最权威的 ADS 培训教程，共包含 10 门 ADS 学习培训课程。课程是由具有多年 ADS 使用经验的微波射频与通信系统设计领域资深专家讲解，并多结合设计实例，由浅入深、详细而又全面地讲解了 ADS 在微波射频电路设计、通信系统设计和电磁仿真设计方面的内容。能让您在最短的时间内学会使用 ADS，迅速提升个人技术能力，把 ADS 真正应用到实际研发工作中去，成为 ADS 设计专家…



课程网址：<http://www.edatop.com/peixun/ads/13.html>

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### HFSS 学习培训课程套装

该套课程套装包含了本站全部 HFSS 培训课程，是迄今国内最全面、最专业的 HFSS 培训教程套装，可以帮助您从零开始，全面深入学习 HFSS 的各项功能和在多个方面的工程应用。购买套装，更可超值赠送 3 个月免费学习答疑，随时解答您学习过程中遇到的棘手问题，让您的 HFSS 学习更加轻松顺畅…

课程网址：<http://www.edatop.com/peixun/hfss/11.html>

## CST 学习培训课程套装

该培训套装由易迪拓培训联合微波 EDA 网共同推出，是最全面、系统、专业的 CST 微波工作室培训课程套装，所有课程都由经验丰富的专家授课，视频教学，可以帮助您从零开始，全面系统地学习 CST 微波工作的各项功能及其在微波射频、天线设计等领域的设计应用。且购买该套装，还可超值赠送 3 个月免费学习答疑…



课程网址: <http://www.edatop.com/peixun/cst/24.html>



## HFSS 天线设计培训课程套装

套装包含 6 门视频课程和 1 本图书，课程从基础讲起，内容由浅入深，理论介绍和实际操作讲解相结合，全面系统的讲解了 HFSS 天线设计的全过程。是国内最全面、最专业的 HFSS 天线设计课程，可以帮助您快速学习掌握如何使用 HFSS 设计天线，让天线设计不再难…

课程网址: <http://www.edatop.com/peixun/hfss/122.html>

## 13.56MHz NFC/RFID 线圈天线设计培训课程套装

套装包含 4 门视频培训课程，培训将 13.56MHz 线圈天线设计原理和仿真设计实践相结合，全面系统地讲解了 13.56MHz 线圈天线的工作原理、设计方法、设计考量以及使用 HFSS 和 CST 仿真分析线圈天线的具体操作，同时还介绍了 13.56MHz 线圈天线匹配电路的设计和调试。通过该套课程的学习，可以帮助您快速学习掌握 13.56MHz 线圈天线及其匹配电路的原理、设计和调试…



详情浏览: <http://www.edatop.com/peixun/antenna/116.html>

## 我们的课程优势:

- ※ 成立于 2004 年，10 多年丰富的行业经验，
- ※ 一直致力并专注于微波射频和天线设计工程师的培养，更了解该行业对人才的要求
- ※ 经验丰富的一线资深工程师讲授，结合实际工程案例，直观、实用、易学

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